

The Size of the Largest Part of Random Weighted Partitions of Large Integers

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Abstract

A weighted partition of the positive integer n is a multiset of size n whose decomposition into a union of disjoint components (parts) satisfies the following condition: for a given sequence of non-negative numbers $\{b_k\}_{k \geq 1}$, a part of size k appears in exactly one of b_k possible types. Assuming that a weighted partition of n is selected uniformly at random from the set of all such partitions, we study the limiting distribution of the largest part size X_n as $n \rightarrow \infty$. Under certain fairly general assumptions on the Dirichlet generating series $D(s) = \sum_{k=1}^{\infty} b_k k^{-s}$, $s = \sigma + iy$, G. Meinardus, *Math. Z.* 59(1954), 388-398, has obtained the asymptotic of the total number of weighted partitions of n . We assume that Meinardus conditions hold and prove that X_n , appropriately normalized, converges weakly to a Gumbel distribution.